The group G is isomorphic to the group labelled by [36, 10] in the Small Groups library.
Ordinary character table of $G \cong$ S3 x S3:

	$1a$	$3a$	$3b$	$3c$	$2a$	$6a$	$2b$	$6b$	$2c$
χ_1	1	1	1	1	1	1	1	1	1
χ_2	1	1	1	1	−1	−1	1	1	−1
χ_3	1	1	1	1	1	1	−1	−1	−1
χ_4	1	1	1	1	−1	−1	−1	−1	1
χ_5	2	−1	2	−1	0	0	2	−1	0
χ_6	2	−1	2	−1	0	0	−2	1	0
χ_7	2	2	−1	−1	2	−1	0	0	0
χ_8	2	2	−1	−1	−2	1	0	0	0
χ_9	4	−2	−2	1	0	0	0	0	0

Trivial source character table of $G \cong$ S3 x S3 at $p = 2$:

Normalisers N_i	N_1				N_2		N_3		N_4	N_5
p-subgroups of G up to conjugacy in G	P_1				P_2		P_3		P_4	P_5
Representatives $n_j \in N_i$	$1a$	$3a$	$3b$	$3c$	$1a$	$3a$	$1a$	$3a$	$1a$	$1a$
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	4	4	4	4	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	4	−2	4	−2	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 1 \cdot \chi_8 + 0 \cdot \chi_9$	4	4	−2	−2	0	0	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 1 \cdot \chi_9$	4	−2	−2	1	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	2	2	2	2	2	2	0	0	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	2	2	−1	−1	2	−1	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	2	2	2	2	0	0	2	2	0	0
$0 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	2	−1	2	−1	0	0	2	−1	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	2	2	2	2	0	0	0	0	2	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_9$	1	1	1	1	1	1	1	1	1	1

$P_1 = Group([()]) \cong 1$
$P_2 = Group([(1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34)]) \cong$ C2
$P_3 = Group([(1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35)]) \cong$ C2
$P_4 = Group([(1,6)(2,3)(4,24)(5,26)(7,19)(8,21)(9,16)(10,18)(11,14)(12,36)(13,15)(17,35)(20,34)(22,33)(23,32)(25,31)(27,30)(28,29)]) \cong$ C2
$P_5 = Group([(1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34), (1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35)]) \cong$ C2 x C2

$N_1 = Group([(1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35), (1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34), (1,4,11)(2,7,16)(3,9,19)(5,12,22)(6,14,24)(8,17,27)(10,20,29)(13,23,31)(15,25,32)(18,28,34)(21,30,35)(26,33,36), (1,5,13)(2,8,18)(3,10,21)(4,12,23)(6,15,26)(7,17,28)(9,20,30)(11,22,31)(14,25,33)(16,27,34)(19,29,35)(24,32,36)]) \cong$ S3 x S3
$N_2 = Group([(1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34), (1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35), (1,13,5)(2,18,8)(3,21,10)(4,23,12)(6,26,15)(7,28,17)(9,30,20)(11,31,22)(14,33,25)(16,34,27)(19,35,29)(24,36,32)]) \cong$ D12
$N_3 = Group([(1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35), (1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34), (1,11,4)(2,16,7)(3,19,9)(5,22,12)(6,24,14)(8,27,17)(10,29,20)(13,31,23)(15,32,25)(18,34,28)(21,35,30)(26,36,33)]) \cong$ D12
$N_4 = Group([(1,6)(2,3)(4,24)(5,26)(7,19)(8,21)(9,16)(10,18)(11,14)(12,36)(13,15)(17,35)(20,34)(22,33)(23,32)(25,31)(27,30)(28,29), (1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35), (1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34)]) \cong$ C2 x C2
$N_5 = Group([(1,2)(3,6)(4,7)(5,18)(8,13)(9,14)(10,26)(11,16)(12,28)(15,21)(17,23)(19,24)(20,33)(22,34)(25,30)(27,31)(29,36)(32,35), (1,3)(2,6)(4,19)(5,10)(7,24)(8,15)(9,11)(12,29)(13,21)(14,16)(17,32)(18,26)(20,22)(23,35)(25,27)(28,36)(30,31)(33,34)]) \cong$ C2 x C2