

The group G is isomorphic to the group labelled by [32, 18] in the Small Groups library.
 Ordinary character table of $G \cong D32$:

	$1a$	$2a$	$2b$	$8a$	$16a$	$2c$	$4a$	$16b$	$16c$	$16d$	$8b$
χ_1	1	1	1	1	1	1	1	1	1	1	1
χ_2	1	-1	-1	1	1	1	1	1	1	1	1
χ_3	1	-1	1	1	-1	1	1	-1	-1	-1	1
χ_4	1	1	-1	1	-1	1	1	-1	-1	-1	1
χ_5	2	0	0	-2	0	2	2	0	0	0	-2
χ_6	2	0	0	0	$E(8) - E(8)^3$	2	-2	$E(8) - E(8)^3$	$-E(8) + E(8)^3$	$-E(8) + E(8)^3$	0
χ_7	2	0	0	0	$-E(8) + E(8)^3$	2	-2	$-E(8) + E(8)^3$	$E(8) - E(8)^3$	$E(8) - E(8)^3$	0
χ_8	2	0	0	$-E(8) + E(8)^3$	$-E(16)^3 + E(16)^5$	-2	0	$E(16)^3 - E(16)^5$	$-E(16) + E(16)^7$	$E(16) - E(16)^7$	$E(8) - E(8)^3$
χ_9	2	0	0	$-E(8) + E(8)^3$	$E(16)^3 - E(16)^5$	-2	0	$-E(16)^3 + E(16)^5$	$E(16) - E(16)^7$	$-E(16) + E(16)^7$	$E(8) - E(8)^3$
χ_{10}	2	0	0	$E(8) - E(8)^3$	$E(16) - E(16)^7$	-2	0	$-E(16) + E(16)^7$	$-E(16)^3 + E(16)^5$	$E(16)^3 - E(16)^5$	$-E(8) + E(8)^3$
χ_{11}	2	0	0	$E(8) - E(8)^3$	$-E(16) + E(16)^7$	-2	0	$E(16) - E(16)^7$	$E(16)^3 - E(16)^5$	$-E(8) + E(8)^3$	

Trivial source character table of $G \cong D32$ at $p = 2$:

Normalisers N_i	N_1	N_2	N_3	N_4	N_5	N_6	N_7	N_8	N_9	N_{10}	N_{11}	N_{12}	N_{13}	N_{14}
p -subgroups of G up to conjugacy in G	P_1	P_2	P_3	P_4	P_5	P_6	P_7	P_8	P_9	P_{10}	P_{11}	P_{12}	P_{13}	P_{14}
Representatives $n_j \in N_i$	1a	1a	1a	1a	1a									
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 2 \cdot \chi_5 + 2 \cdot \chi_7 + 2 \cdot \chi_8 + 2 \cdot \chi_{10} + 2 \cdot \chi_{11}$	32	0	0	0	0	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 2 \cdot \chi_5 + 2 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	16	16	0	0	0	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 1 \cdot \chi_7 + 1 \cdot \chi_8 + 1 \cdot \chi_{10} + 1 \cdot \chi_{11}$	16	0	2	0	0	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 1 \cdot \chi_7 + 1 \cdot \chi_8 + 1 \cdot \chi_{10} + 1 \cdot \chi_{11}$	16	0	0	2	0	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 2 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	8	8	0	0	8	0	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	8	8	2	0	0	2	0	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 1 \cdot \chi_6 + 1 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	8	8	0	2	0	0	2	0	0	0	0	0	0	0
$1 \cdot \chi_1 + 1 \cdot \chi_2 + 1 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	4	4	0	0	4	0	0	4	0	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	4	4	2	0	4	2	0	0	2	0	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 1 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	4	4	0	2	4	0	2	0	0	2	0	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 1 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	2	2	2	0	2	2	0	2	2	0	2	0	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 1 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	2	2	0	2	2	0	2	2	0	2	0	2	0	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	2	2	0	0	2	0	0	2	0	0	0	0	2	0
$1 \cdot \chi_1 + 0 \cdot \chi_2 + 0 \cdot \chi_3 + 0 \cdot \chi_4 + 0 \cdot \chi_5 + 0 \cdot \chi_6 + 0 \cdot \chi_7 + 0 \cdot \chi_8 + 0 \cdot \chi_{10} + 0 \cdot \chi_{11}$	1	1	1	1	1	1	1	1	1	1	1	1	1	1

$P_1 = \text{Group}([[]]) \cong 1$

$P_2 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(27, 32)]) \cong C_2$

$P_3 = \text{Group}([(1, 3)(2, 7)(4, 23)(5, 25)(6, 13)(8, 27)(9, 29)(10, 19)(11, 14)(12, 16)(15, 31)(17, 20)(18, 22)(21, 32)(24, 26)(28, 30)]) \cong C_2$

$P_4 = \text{Group}([(1, 2)(3, 17)(4, 20)(5, 22)(6, 10)(7, 11)(8, 14)(9, 16)(12, 32)(13, 28)(15, 30)(18, 31)(19, 24)(21, 26)(23, 29)(25, 27)]) \cong C_2$

$P_5 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(27, 32)]) \cong C_4$

$P_6 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(20, 30)(23, 31)(27, 32)]) \cong C_2 \times C_2$

$P_7 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(20, 30)(23, 31)(25, 27)]) \cong C_2 \times C_2$

$P_8 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(27, 32)]) \cong C_8$

$P_9 = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(27, 32)]) \cong D_8$

$P_{10} = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(25, 27)]) \cong D_8$

$P_{11} = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(20, 30)(23, 31)(25, 27)]) \cong D_{16}$

$P_{12} = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(20, 30)(23, 31)(25, 27)]) \cong D_{16}$

$P_{13} = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(25, 27)]) \cong C_{16}$

$P_{14} = \text{Group}([(1, 6)(2, 10)(3, 13)(4, 15)(5, 16)(7, 19)(8, 21)(9, 22)(11, 24)(12, 25)(14, 26)(17, 28)(18, 29)(20, 30)(23, 31)(25, 27)]) \cong D_{32}$

$N_1 = \text{Group}([(1, 2)(3, 17)(4, 20)(5, 22)(6, 10)(7, 11)(8, 14)(9, 16)(12, 32)(13, 28)(15, 30)(18, 31)(19, 24)(21, 26)(23, 29)(25, 27)]) \cong D_{32}$

$N_2 = \text{$